

**APPLICATION**

# The R package divDyn for quantifying diversity dynamics using fossil sampling data

Ádám T. Kocsis<sup>1,2</sup> | Carl J. Reddin<sup>1</sup> | John Alroy<sup>3</sup> | Wolfgang Kiessling<sup>1</sup> <sup>1</sup>GeoZentrum Nordbayern, Universität Erlangen-Nürnberg, Erlangen, Germany<sup>2</sup>MTA-MTM-ELTE Research Group for Paleontology, Budapest, Hungary<sup>3</sup>Department of Biological Sciences, Macquarie University, Sydney, New South Wales, Australia**Correspondence**Ádám T. Kocsis  
Email: adam.kocsis@fau.de**Funding information**

Deutsche Forschungsgemeinschaft, Grant/Award Number: Ko 5382/1-1, Ko 5382/1-2, Ki 806/16-1 and FO 2332

Handling Editor: Samantha Price

**Abstract**

1. Unbiased time series of diversity dynamics are vital for quantifying the grand history of life. Applications include identifying ancient mass extinctions and inferring both biotic and abiotic controls on diversification rates.
2. We introduce divDyn, a new R package that facilitates the calculation of taxonomic richness, extinction and origination rates from time-binned fossil data. State-of-the-art counting protocols, and sampling standardization functions permit the reconstruction of biologically meaningful time series. Additional functions permit the partitioning of turnover rates by environmental affinity.
3. Using divDyn, we display Phanerozoic-scale diversity dynamics of marine invertebrates. With the help of the core function and standard subsampling options, we revisit the hypothesis of declining taxonomic rates over time, mass extinctions and equilibrium diversity dynamics and assess their methodological dependency. Our results suggest that rates declined only over the early Phanerozoic, only three mass extinctions stand out clearly, and evidence of equilibrium dynamics is dependent on the used methods.
4. The modular and fast implementation of published methods ensures traceability, reproducibility and comparability of future studies.

**KEYWORDS**

diversity dynamics, extinction, fossil record, origination, Palaeobiology Database, subsampling

## 1 | INTRODUCTION

Temporal trajectories of global diversity (Alroy, 2010a; Alroy et al., 2001, 2008; Sepkoski, Bambach, Raup, & Valentine, 1981) as well as extinction and origination rates (Alroy, 2008, 2014, 2015; Bambach, Knoll, & Wang, 2004; Benton, 1995; Carr & Kitchell, 1980; Foote, 2000; Newell, 1952; Raup & Sepkoski, 1982; Sepkoski, 1993) have led to the recognition of ancient mass extinctions (Alroy, 2008; Raup & Sepkoski, 1982) and major insights about the interplay of evolutionary crisis and recovery. Calculating these time series from an incomplete fossil record is a fundamental task, as they underpin the statistical testing of grand questions in macroevolution.

Early studies largely relied on compendia of stratigraphic ranges, deriving diversity metrics from overlapping durations of taxa (e.g.

Sepkoski, 1984). Since the advent of the Palaeobiology Database (PaleoDB; <https://paleobiodb.org>) diversity dynamics have largely been inferred from occurrence datasets that incorporate hundreds of thousands of items (Alroy, 2008, 2010a; Alroy et al., 2001). Occurrence data allow for alternative counting methods and sampling standardization but implementing these methods in scripting languages is time-consuming and can be challenging for students and researchers with little programming experience. The algorithmic implementation of some procedures and the multiple steps of data filtering also permit considerable analytical freedom, which potentially compromises the comparability and traceability of results. Although there are novel alternatives to turnover rate calculation (e.g. the Bayesian approach of the PyRATE package, Silvestro, Salamin, & Schnitzler, 2014), a standardized toolkit for the traditional methods will facilitate a fast and

consistent workflow and allow researchers to focus on scientific questions rather than losing time with the repeated implementation of established methods.

Here, we present the R (R Development Core Team, 2018) package `divDyn`, which facilitates the calculation of diversity dynamics from fossil occurrence datasets. Our purpose is to establish a transparent, traceable and modular workflow from data acquisition to the calculation of biologically meaningful diversity metrics. The primary application of the package is expected to be for data from the PaleoDB, the largest macrofossil occurrence dataset available. However, any dataset for which diversity metrics are to be assessed in temporal or spatial intervals can also be processed with `divDyn`. Examples are the Neotoma Paleocology Database (Williams et al., 2018), Neptune (Lazarus, 1994), and AMMON (Korn & Ilg, 2007) databases. To demonstrate the benefits of `divDyn`, we revisit results from an earlier study on Phanerozoic-scale diversity dynamics (Alroy, 2008).

## 2 | FEATURES

### 2.1 | Calculation of time series

To prepare an occurrence dataset for analysis in `divDyn`, it must be formatted as a table with each row representing a single occurrence of a taxon (Table 1). The core function `divDyn()` calculates taxonomic richness, extinction and origination rate

**TABLE 1** Format of the data (from the Palaeobiology Database) accepted by the main functions of the package

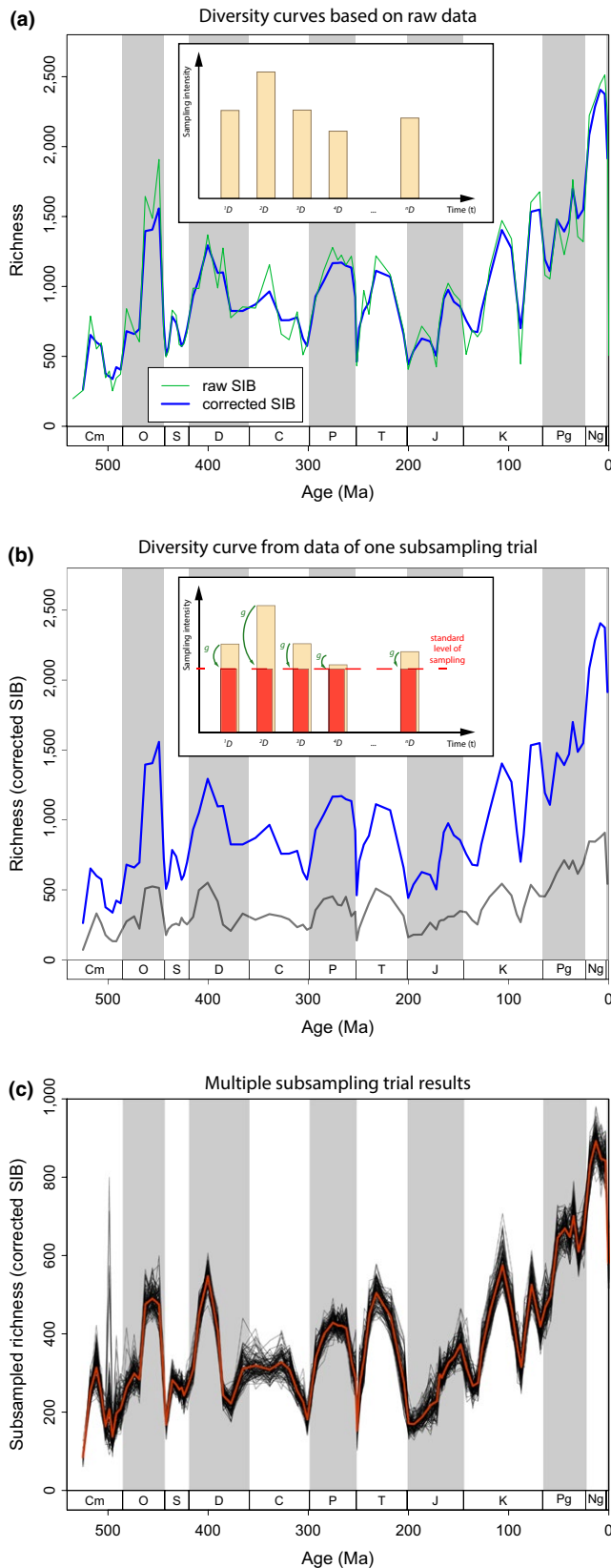
tax	bin	coll	lat	lng
<i>Turbinaria</i>	89	22,968	43.55	-3.82
<i>Lithophyllia</i>	89	22,968	43.55	-3.82
<i>Caryophyllia</i>	89	22,968	43.55	-3.82
<i>Trochocyathus</i>	89	22,968	43.55	-3.82
<i>Favia</i>	91	22,969	46.01	15.36
<i>Solenastrea</i>	91	22,969	46.01	15.36
<i>Tarbellastraea</i>	91	22,969	46.01	15.36
<i>Mussismilia</i>	91	22,969	46.01	15.36
<i>Goniopora</i>	90	22,971	18.09	-61.93
<i>Porites</i>	90	22,971	18.09	-61.93

*Note.* The `tax` variable includes the taxon names of the occurrences and `bin` indicates time (mandatory variables). Occurrences should be assigned to discrete time intervals (bins), but a continuous time-related dimension (e.g. years before present, or metres in a section) will be translated to discrete bins by the package. Time flows from smaller to larger numbers by default.

estimates using the presence-absence patterns of the time bin-taxon matrix implied by the input dataset. It calculates a large suite of diversity metrics and rates in one go, ranging from classical sampled-in-bin richness to the recent extinction and origination rates (Table 2).

**TABLE 2** Variables output by the main function of the package

Variable name	Metric name	Type	Reference
<code>tSing</code> , <code>tOri</code> , <code>tExt</code> , <code>tThrough</code>	Range-based taxon patterns	Counts	Foote (1999)
<code>t2d</code> , <code>t2u</code> , <code>t3</code> , <code>tPart</code> , <code>tGFu</code> , <code>tGFd</code>	Occurrence-based taxon patterns	Counts	Alroy (2008, 2014)
<code>extProp</code> , <code>oriProp</code>	Proportional extinctions and originations	Turnover	Newell (1952)
<code>extPC</code> , <code>oriPC</code>	Per capita extinction and origination rates	Turnover	Foote (1999); Alroy (1996)
<code>ext3t</code> , <code>ori3t</code>	Three-timer extinction and origination rates	Turnover	Alroy (2008)
<code>extC3t</code> , <code>oriC3t</code>	Corrected three-timer extinction and origination rates	Turnover	Alroy (2008)
<code>extGF</code> , <code>oriGF</code>	Gap-filler extinction and origination rates	Turnover	Alroy (2014)
<code>ext2f3</code> , <code>ori2f3</code>	Second-for-third substitution extinction and origination rates	Turnover	Alroy (2015)
<code>divSIB</code>	Sampled-in-bin diversity (SIB)	Richness	Miller and Foote (1996)
<code>divRT</code>	Range-through diversity (RT)	Richness	Newell (1952)
<code>divBC</code>	Boundary-crosser diversity (BC)	Richness	Carr and Kitchell (1980)
<code>divCSIB</code>	Corrected sampled-in-bin diversity	Richness	Alroy et al. (2008)
<code>samp3t</code>	Three-timer sampling completeness	Sampling completeness	Alroy (2008)
<code>sampRange</code>	Range-based sampling completeness	Sampling completeness	Foote and Miller (2007)



**FIGURE 1** Demonstration of the procedures implemented in the subsampling wrapper function. (a) Calculation of raw results, (b) calculation of results from a single subsampling trial and (c) multiple trial results and averaging.  $^nD$  represents a bin-specific subset of the data and  $g$  is the subsampling function. The curves show genus richness from the Phanerozoic example dataset, standardized with Shareholder Quorum Subsampling (SQS) at the stratigraphic resolution of geologic stages. Blue line on panel (b) is the same as on (a), red line (c) indicates the mean of the trials. The number of iterations was 100, the quorum for SQS is 0.7

group of methods in this field of research, uses interpolation to answer the general question, “What would the results look like if fewer data were available?”. Implementations of these methods are available for estimating richness from an incomplete sample (Hammer, Harper, & Ryan, 2001; Hsieh, Ma, & Chao, 2016), but their application is more complicated in the context of time-series reconstruction (Figure 1), where information is aggregated in multiple time bins.

We formalized the subsampling process in the versatile wrapper function `subsampling()`. If the dataset is divisible to time bin-specific parts, a subsampling function can be applied to each of them, so the resulting subsets feature the same sampling characteristics (for instance, intensity). The desired result is then a function (`FUN`) of this abstract dataset, which can be approximated by generating multiple, random subsamples and allowing the emerging variation to propagate to the results of `FUN`.

The advantage of this formalization is that `FUN` can be any user-provided function that is applicable to the original dataset, with any sort of output, such as vectors (time series) and complex structures. In the case of primitive trial results (vectors and matrices), the averaging of time series can be automated. The package currently features Classical Rarefaction (CR; Miller & Foote, 1996; Sanders, 1968), Occurrence-Weighted By-List Subsampling (O<sup>W</sup>; Alroy et al., 2001), and Shareholder Quorum Subsampling (SQS; Alroy, 2010a).

### 2.3 | Additional functionality

To facilitate the stratigraphic assignment of collections from the PaleoDB, we compiled tables using the dynamic time-scale interpreter of Fossilworks (<http://fossilworks.org/>) that links entries to major geochronological intervals of two predefined time-scales (the level of geological stages and the 10-million-year [Myr] time-scale). Additional tables are also provided to categorize the downloaded occurrences in terms of bathymetry (shallow, deep), substrate (siliciclastic vs. carbonate) and reef vs. non-reef environments, which are useful for the calculation of environmental preferences (`affinity()` function) and extinction selectivity (KieSSLing & Kocsis, 2015).

The `divDyn()` function creates output in discretized time intervals. Results can be visualized effectively with the additional plotting functions that display the used time-scale (`tsplot()`), stratigraphic ranges (`ranges()`) or changes in composition (`parts()`). The basic functionality of the package is elaborated in the accompanying

### 2.2 | Sampling standardization procedures

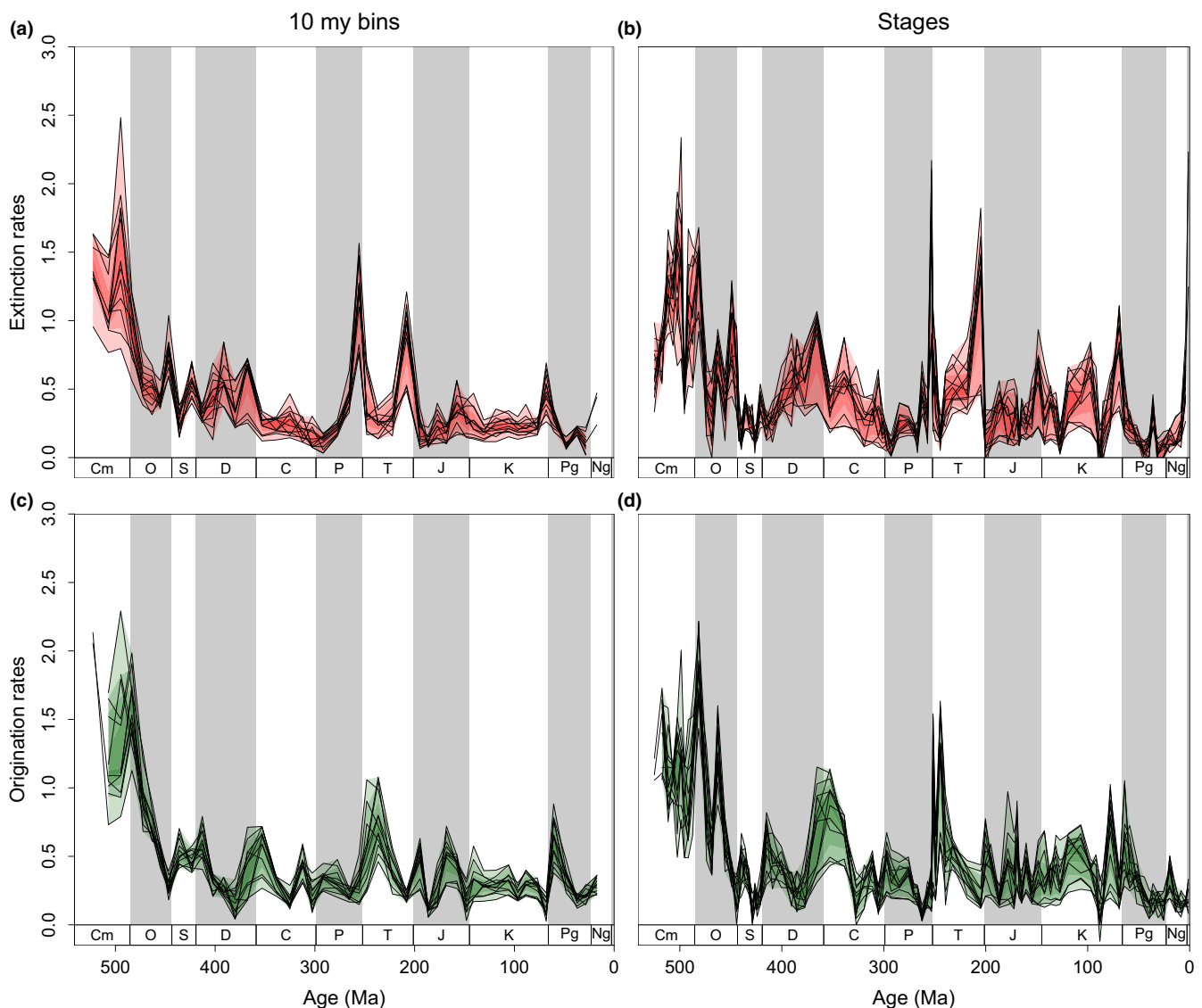
Sampling standardization is a useful tool for reducing the bias of changing sampling intensity. Subsampling, the most common

vignette (Handout to the R package *divDyn*), with an example dataset of scleractinian corals used by Kiessling and Kocsis (2015).

### 3 | EXAMPLE APPLICATION: PHANEROZOIC-SCALE DIVERSITY DYNAMICS OF MARINE ANIMALS

Tracing diversity through the entire Phanerozoic (the last 541 Myr of Earth history) has been a focus of palaeobiological research since the first global diversity curves were published (Newell, 1952). The temporal decline of turnover rates has largely gone unchallenged since its first observation (Raup & Sepkoski, 1982), whereas the original “Big Five” mass extinction events of Raup and Sepkoski (1982) have been repeatedly revisited, with different conclusions (Alroy, 2008;

Bambach et al., 2004). Much discussion has focused on the dramatic rise of marine biodiversity over the last 100 Myr, which is evident in older compilations (Sepkoski, 1993; Valentine, 1970) but much less so in sampling-standardized analyses (Alroy et al., 2008). Not yet formally contested are Alroy's (2008, 2010b) analyses of the temporal relationship between diversity and rates. If these results are robust at different temporal resolutions, they strongly argue for equilibrial, diversity-dependent diversity dynamics (Alroy, 1996; Sepkoski, 1978, 1984). With the continuous expansion of both fossil occurrence datasets and the toolkit to analyse them, it is necessary to re-evaluate such scientific outcomes on a periodical basis. The objective of this case study is to assess the robustness of previous results in the face of the increase in the number of fossil occurrences and the number of analytical choices we face when we express diversity dynamics over deep time.



**FIGURE 2** Genus-level Phanerozoic-scale extinction (a,b) and origination rates (c,d) calculated at the level of 10 million-year (Myr) bins (a,c) and stratigraphic stages (b,d). Each panel features 12 (3 treatment  $\times$  4 rate metrics) curves, either raw, CR (quotas are 4,800 occurrences for the 10 Myr bins and 1,100 for the stages) or Shareholder Quorum Subsampling-standardized (quorum is 0.7 for both) average per capita rates, corrected three-timer rates, gap-filler rates or second-for-third substitution rates

**TABLE 3** Results from method-specific outcomes of the time-series calculations for 10 million-year (Myr) bins (a) and stages (b)

		10 Myr time-scale											
		Raw					SQS						
(a)		PC	C3t	GF	2f3	PC	C3t	GF	2f3	PC	C3t	GF	2f3
Pulsed/continuous	ext. rates with durations	-0.43	-0.44	-0.35	-0.32	-0.56	-0.58	-0.56	-0.58	-0.41	-0.46	-0.32	-0.35
	norm. ext. rates with durations	0.29	-0.42	0.29		-0.35	-0.41			0.31			
Declines	orig. rates with durations	<u>0.57</u>	<u>0.58</u>	<u>0.59</u>	<u>0.5</u>	<u>0.55</u>	<u>0.6</u>	<u>0.61</u>	<u>0.55</u>	<u>0.58</u>	<u>0.59</u>	<u>0.64</u>	<u>0.54</u>
	post-Ordovician extinctions	0.38	0.4	0.4		0.44	0.44	0.42		0.37	0.42	0.42	0.45
	originations	<u>0.53</u>	<u>0.44</u>	<u>0.47</u>	<u>0.45</u>	<u>0.55</u>	<u>0.44</u>	<u>0.48</u>	<u>0.47</u>	<u>0.55</u>	<u>0.43</u>	<u>0.49</u>	<u>0.45</u>
	post-Ordovician originations												
Mass extinctions	end-Permian ME	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
	end-Triassic ME	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
	end-Cretaceous ME	Yes	Yes	Yes	Yes	No	Yes	Yes	Yes	No	Yes	No	No
	end-Permian is highest	Yes	No	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Rate distribution	number of mass extinctions	5	3	4	4	2	4	3	3	2	3	2	2
	extinctions log-normal (p-values)			0.049			0.029						
	originations log-normal (p-values)				0.002							0.035	0.048
Equilibrium dynamics	origination and lagged diversity				0.34					0.41			
	diversity and lagged extinction	0.44			0.35					0.43			
	extinction and lagged origination		<u>0.55</u>			<u>0.68</u>	<u>0.42</u>	<u>0.42</u>	0.36		<u>0.49</u>		

(Continues)



### 3.1 | Data processing and applied methods

The analyses presented in this section can be reproduced with the second vignette accompanying the package (Supporting Information). The data used here were downloaded from the PaleoDB on January 3, 2019, including all occurrences from the Ediacaran to the Holocene. The data were filtered to marine taxa and binned to geological stages as well as the often-used 10 Myr bins (Alroy et al., 2008). As the procedural treatment of stages in the Cambrian and Ordovician systems was influenced by considerable stratigraphic error, they were resolved using biozone and formation entries (Ordovician), and with data from previous analyses (Cambrian, Na & Kiessling, 2015). Following related literature, all analyses were carried out at the genus level. However, species-level analyses can be conducted with the same procedures.

We computed diversity dynamics at both stratigraphic resolutions (stages and 10 Myr), with three different treatments of the data (raw, CR and SQS). Four different rate metrics were applied: per capita rates (Foote, 1999; most prevalent in previous studies), corrected three-timer rates (Alroy, 2008), gap-filler equations (Alroy, 2014) and second-for-third substitution rates of Alroy (2015). This resulted in 24 different sets (2 time-scales  $\times$  3 data treatments  $\times$  4 rate metrics) of richness, origination and extinction rate series, each affected in a different way by the distorting effects of incomplete, heterogeneous sampling and estimation error.

As indicated by Foote (2005), most taxonomic turnover was probably pulsed, likely at stage boundaries. This assertion is supported by the infrequent correlations between interval durations and rate values when the time dimension is excluded from the rate equations (Table 3 and Alroy, 2008). For the analysis of distributions, outliers and cross correlations, we detrended the rates and the richness by applying LOESS with AICc-based smoothing parameters (Wang, 2010) to describe long-term variation (Bambach et al., 2004). Mass extinctions are defined as statistical outliers (using boxplot statistics) after removing the long-term trend.

### 3.2 | Results

The first order patterns match well across different methods but the estimates for the individual time slices (Figure 2), and thus the support of the hypotheses (Table 3), may vary considerably. Although a decline of extinction and origination rates is supported if the Cambrian and Ordovician are included in the dataset, these rates are unlikely to have featured a solid decline after the Ordovician period. All detrended extinction rate series feature the latest Permian value as a mass extinction, which is consistently the highest value in the series. The number of mass extinctions varies among analyses. Of the traditional “Big Five” mass extinctions (Raup & Sepkoski, 1982), the end-Triassic and the end-Cretaceous values also usually show up as outliers, as was indicated by Alroy (2008). Equilibrial dynamics, however, received varying support with the different methods and time-scales.

### 3.3 | Discussion

Most major results derived from the Phanerozoic-scale analyses of the marine animal fossil record are robust after the additional 10 years of data entry and methodological development since Alroy (2008). Sepkoski (1993) found similar robustness in analysing his older, range-based dataset. One notable exception is the decline of rates through time, which receives varying support if the first two Phanerozoic periods are excluded, suggesting more stationary turnover after the extinction of high-turnover clades by the mid-Ordovician. Our results support a more continuous transition between background and mass extinction and are more consistent with a “Big Three” (Alroy, 2008; Bambach et al., 2004) rather than a “Big Five” (Raup & Sepkoski, 1982) scenario. Likewise, changing how the data are treated either questions equilibrial diversity dynamics or suggests that carrying capacities change over time (Alroy, 2010b; Marshall & Quental, 2016; Sepkoski, 1984).

Whichever the case, using a standard toolkit like *divDyn* enhances our ability to reproduce previous results and test the effect of added data, changing temporal resolution, or alternative methods. We hope that our package will spur large-scale diversity analyses beyond the still small group of trained peers. We intend to expand the set of output variables in the future, for instance, by adding interfaces to the *PyRATE* (Silvestro et al., 2014) program and implementations of capture–mark–recapture (Liow & Nichols, 2010) approaches.

### ACKNOWLEDGEMENTS

The study was funded by the Deutsche Forschungsgemeinschaft (Ko 5382/1-1, Ko 5382/1-2 and Ki 806/16-1) and is part of the Research Unit TERSANE (FO 2332). The authors are grateful to Na Lin for assigning the Cambrian collections to stages. Discussions with M. Steinbauer, E. Jarochowska, J. Pálffy, R. Benson and G. Antell helped in the development of the package, as did the feedback from the first year Master in Palaeobiology students at FAU. Comments of two anonymous reviewers greatly improved the paper. This is Paleobiology Database publication no 335.

### AUTHORS' CONTRIBUTIONS

A.T.K. conceived the project, wrote the first manuscript draft and the software using code from W.K. and J.A. as foundations. W.K. and C.J.R. contributed to testing, interface and feature development, as well as the debugging of code. All authors contributed to writing the manuscript.

### DATA ACCESSIBILITY

The package is accessible from the CRAN servers (<https://CRAN.R-project.org/package=divDyn>) and from its GitHub repository. The occurrence data used here are freely available from the Paleobiology Database (<https://paleobiodb.org/data1.2/occs/list.cs>)

v?interval=Ediacaran,Holocene&show=class,classex,genus,subgenus,abund,coll,coords,loc,paleoloc,strat,stratext,lith,env,ref,crmod,timebins,timecompare). All files needed to reproduce the example are available on GitHub (archived in Zenodo, <https://doi.org/10.5281/zenodo.2545982>).

## ORCID

Ádám T. Kocsis  <http://orcid.org/0000-0002-9028-665X>

John Alroy  <http://orcid.org/0000-0002-9882-2111>

Carl J. Reddin  <https://orcid.org/0000-0001-5930-1164>

Wolfgang Kiessling  <https://orcid.org/0000-0002-1088-2014>

## REFERENCES

- Alroy, J. (1996). Constant extinction, constrained diversification, and uncoordinated stasis in North American mammals. *Palaeogeography, Palaeoclimatology, Palaeoecology*, 127, 285–311. [https://doi.org/10.1016/S0031-0182\(96\)00100-9](https://doi.org/10.1016/S0031-0182(96)00100-9)
- Alroy, J. (2008). Dynamics of origination and extinction in the marine fossil record. *Proceedings of the National Academy of Sciences of the United States of America*, 105, 11536–11542. <https://doi.org/10.1073/pnas.0802597105>
- Alroy, J. (2010a). The shifting balance of diversity among major marine animal groups. *Science*, 329, 1191–1194. <https://doi.org/10.1126/science.1189910>
- Alroy, J. (2010b). Geographical, environmental and intrinsic biotic controls on Phanerozoic marine diversification. *Palaeontology*, 53, 1211–1235. <https://doi.org/10.1111/j.1475-4983.2010.01011.x>
- Alroy, J. (2014). Accurate and precise estimates of origination and extinction rates. *Paleobiology*, 40, 374–397. <https://doi.org/10.1666/13036>
- Alroy, J. (2015). A more precise speciation and extinction rate estimator. *Paleobiology*, 41, 633–639. <https://doi.org/10.1017/pab.2015.26>
- Alroy, J., Aberhan, M., Bottjer, D. J., Foote, M., Fürsich, F. T., Harries, P. J., ... Visaggi, C. C. (2008). Phanerozoic trends in the global diversity of marine invertebrates. *Science*, 321, 97–100. <https://doi.org/10.1126/science.1156963>
- Alroy, J., Marshall, C. R., Bambach, R. K., Bezusko, K., Foote, M., Fürsich, F. T., ... Webber, A. (2001). Effects of sampling standardization on estimates of Phanerozoic marine diversification. *Proceedings of the National Academy of Sciences of the United States of America*, 98, 6261–6266. <https://doi.org/10.1073/pnas.111144698>
- Bambach, R. K., Knoll, A. H., & Wang, S. C. (2004). Origination, extinction, and mass depletions of marine diversity. *Paleobiology*, 30, 522–542. [https://doi.org/10.1666/0094-8373\(2004\)030<0522:OEAMDO>2.0.CO;2](https://doi.org/10.1666/0094-8373(2004)030<0522:OEAMDO>2.0.CO;2)
- Benton, M. J. (1995). Diversification and extinction in the history of life. *Science*, 268, 52–58. <https://doi.org/10.1126/science.7701342>
- Carr, T. R., & Kitchell, J. A. (1980). Dynamics of taxonomic diversity. *Paleobiology*, 6, 427–443. <https://doi.org/10.1017/S0094837300003602>
- Foote, M. (1999). Morphological diversity in the evolutionary radiation of Paleozoic and post-Paleozoic crinoids. *Paleobiology*, 25, 1–115. <https://doi.org/10.1017/S0094837300020236>
- Foote, M. (2000). Origination and extinction components of taxonomic diversity: General problems. *Paleobiology*, 26, 74–102. [https://doi.org/10.1666/0094-8373\(2000\)26\[74:OAEOT\]2.0.CO;2](https://doi.org/10.1666/0094-8373(2000)26[74:OAEOT]2.0.CO;2)
- Foote, M. (2005). Pulsed origination and extinction in the marine realm. *Paleobiology*, 31, 6–20. [https://doi.org/10.1666/0094-8373\(2005\)031<0006:POAEIT>2.0.CO;2](https://doi.org/10.1666/0094-8373(2005)031<0006:POAEIT>2.0.CO;2)
- Foote, M., & Miller, A. I. (2007). *Principles of paleontology*. New York, NY: W. H. Freeman and Company.
- Hammer, O., Harper, D. A. T., & Ryan, P. D. (2001). PAST: Paleontological statistics software package for education and data analysis. *Paleontologica Electronica*, 4, 9.
- Hsieh, T. C., Ma, K. H., & Chao, A. (2016). iNEXT: An R package for rarefaction and extrapolation of species diversity (Hill numbers). *Methods in Ecology and Evolution*, 7, 1451–1456. <https://doi.org/10.1111/2041-210X.12613>
- Kiessling, W., & Kocsis, Á. T. (2015). Biodiversity dynamics and environmental occupancy of fossil azoocanthellate and zooecanthellate scleractinian corals. *Paleobiology*, 41, 402–414. <https://doi.org/10.1017/pab.2015.6>
- Korn, D., & Ilg, A. (2007). AMMON. Retrieved from <http://www.wahrestarke.com/ammon/>
- Lazarus, D. (1994). Neptune: A marine micropaleontology database. *Mathematical Geology*, 26, 817–832. <https://doi.org/10.1007/BF02083119>
- Liow, L. H., & Nichols, J. D. (2010). Estimating rates and probabilities of origination and extinction using taxonomic occurrence data: Capture-mark-recapture (CMR) approaches. In J. Alroy & G. Hunt (Eds.), *Quantitative methods in paleobiology* (pp. 81–94). Lubbock, TX: The Paleontological Society.
- Marshall, C. R., & Quental, T. B. (2016). The uncertain role of diversity dependence in species diversification and the need to incorporate time-varying carrying capacities. *Philosophical Transactions of the Royal Society B*, 371, 20150217. <https://doi.org/10.1098/rstb.2015.0217>
- Miller, A. I., & Foote, M. (1996). Calibrating the Ordovician radiation of marine life: Implications for Phanerozoic diversity trends. *Paleobiology*, 22, 304–309. <https://doi.org/10.1017/S0094837300016237>
- Na, L., & Kiessling, W. (2015). Diversity partitioning during the Cambrian radiation. *Proceedings of the National Academy of Sciences of the United States of America*, 112, 4702–4706. <https://doi.org/10.1073/pnas.1424985112>
- Newell, N. D. (1952). Periodicity in invertebrate evolution. *Journal of Paleontology*, 26, 371–385.
- R Development Core Team. (2018). *R: A language and environment for statistical computing*. Vienna, Austria: R Foundation for Statistical Computing.
- Raup, D. M., & Sepkoski, J. J. (1982). Mass extinctions in the marine fossil record. *Science*, 215, 1501–1503. <https://doi.org/10.1126/science.215.4539.1501>
- Sanders, H. L. (1968). Marine benthic diversity: A comparative study. *The American Naturalist*, 102, 243–282. <https://doi.org/10.1086/282541>
- Sepkoski, Jr., J. J. (1978). A kinetic model of Phanerozoic taxonomic diversity I. Analysis of marine orders. *Paleobiology*, 4, 223–251. <https://doi.org/10.1017/S0094837300005972>
- Sepkoski, Jr., J. J. (1984). A kinetic model of Phanerozoic taxonomic diversity. III. Post-Paleozoic families and mass extinctions. *Paleobiology*, 10, 246–267. <https://doi.org/10.1017/S0094837300008186>
- Sepkoski, J. J. (1993). Ten years in the library: New data confirm paleontological patterns. *Paleobiology*, 19, 43–51. <https://doi.org/10.1017/S0094837300012306>
- Sepkoski, J. J., Bambach, R. K., Raup, D. M., & Valentine, J. W. (1981). Phanerozoic marine diversity and the fossil record. *Nature*, 293, 435–437. <https://doi.org/10.1038/293435a0>
- Silvestro, D., Salamin, N., & Schnitzler, J. (2014). PyRate: A new program to estimate speciation and extinction rates from incomplete fossil data. *Methods in Ecology and Evolution*, 5, 1126–1131. <https://doi.org/10.1111/2041-210X.12263>
- Valentine, J. W. (1970). How many marine invertebrate fossil species? A new approximation. *Journal of Paleontology*, 44, 410–415.
- Wang, X.-F. (2010). *fANCOVA: Nonparametric analysis of covariance*. Retrieved from <https://CRAN.R-project.org/package=fANCOVA>
- Williams, J. W., Grimm, E. C., Blois, J. L., Charles, D. F., Davis, E. B., Goring, S. J., ... Takahara, H. (2018). The Neotoma Paleocology Database, a multiproxy, international, community-curated data resource. *Quaternary Research*, 89, 156–177. <https://doi.org/10.1017/qua.2017.105>



## SUPPORTING INFORMATION

Additional supporting information may be found online in the Supporting Information section at the end of the article.

**How to cite this article:** Kocsis ÁT, Reddin CJ, Alroy J, Kiessling W. The R package divDyn for quantifying diversity dynamics using fossil sampling data. *Methods Ecol Evol.* 2019;10:735–743. <https://doi.org/10.1111/2041-210X.13161>